#### UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

# MARK SCHEME for the October/November 2009 question paper for the guidance of teachers

## 9709 MATHEMATICS

9709/42

Paper 42, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the October/November 2009 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.



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### **Mark Scheme Notes**

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

## **Penalties**

- MR −1 A penalty of MR −1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR −2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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1	(i)	[P = Wsin40°]	M1		For resolving forces parallel to the plane or for a correct triangle of forces or for resolving horizontally and vertically
		P = 7.71	A1	2	, 42.24
	(ii)	$[P\cos 40^{\circ} = W\sin 40^{\circ}]$ P = 10.1	M1 A1	2	
2	(i)	Loss in PE is $2.7 \times 10^6$ J	B1	1	
	(ii)	WD is $2.1 \times 10^6$ J	B1ft	1	ft incorrect loss in PE
	(iii)	KE change = $\frac{1}{2} 15000(16^2 - 14^2)$ [WD = $\frac{1}{2} 15000(16^2 - 14^2) + 1600 \times 2500$ ] WD is $4.45 \times 10^6$ J	B1 M1 A1	3	WD by DF = Gain in KE + WD by resistance
					SR for candidates who use Newton's Law method instead of energy (max 1/3) $a = (16^2 - 14^2)/(2 \times 2500) = 0.012$ DF = $1600 + 15000 \times 0.012 = 1780$ WD = $1780 \times 2500 = 4.45 \times 10^6$ B1
3	(i)	[DF = 600 at max speed] [DF = 24000/v] Speed cannot exceed 40 ms <sup>-1</sup>	M1 M1 A1	3	For using DF = R at max. speed For using DF = $P/V$ AG
	(ii)	DF – R = ma] 24000/15 - 600 = 1250a Acceleration is 0.8 ms <sup>-2</sup>	M1 A1 A1	3	For using Newton's second law
4	(i)	$[1.2 = mg \cos\alpha]$ Mass is 0.125 kg	M1 A1	2	For resolving forces normal to the plane
	(ii)	[-mg sinα - F = ma] - 0.125 × 10 × 0.28 - 0.4 = 0.125a a = -6 → deceleration is 6 ms <sup>-2</sup>	M1 A1ft A1	3	For using Newton's second law ft incorrect mass
	(iii)		M1		For comparing magnitudes of $\mu R$ (0.4) and mg sin $\alpha$ (0.35)
		$\mu$ R > mg sin $\alpha$ $\rightarrow$ particle remains at rest	A1	2	

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5	(i)		1/1		For regulating forces wertically
5	(i)	$12 + 15\sin 30^{\circ} = R$	M1 A1		For resolving forces vertically
		$F = 15\cos 30^{\circ}$	B1		
			M1		For using $\mu = E/D$
		$[\mu = 15\cos 30^{\circ}/(12 + 15\sin 30^{\circ})]$ Coefficient is 0.666		5	For using $\mu = F/R$
		Coefficient is 0.000	A1	5	AG
	(ii)	$F = 0.666(12 - 15\sin 30^{\circ})$	B1		
			M1		For using Newton's second law
		$15\cos 30^{\circ} - F = 1.2a$	A1		
		Acceleration is 8.33 ms <sup>-2</sup>	A1	4	
6	(i)				For applying Newton's second law to A
U	(1)				or to B or for using
			M1		(M + m)a = (M - m)g
		T - 0.3g = 0.3a and $0.7g - T = 0.7a$ or	A1		(171 · 111)a (171 · 111)g
		(0.7 + 0.3)a = (0.7 - 0.3)g	111		
		(0.7 + 0.5)a - (0.7 - 0.5)g Acceleration is 4 ms <sup>-2</sup>	A1	3	
		Acceleration is 7 mis	Α1	5	
	(ii)	$s_1 = 1.6^2/(2 \times 4)$	B1ft		ft acceleration
	( )	. ,	M1		For using $0^2 = 1.6^2 - 2gs_2$
		Height is 0.448 m	A1	3	From $s_1 + s_2 = 0.32 + 0.128$
	(iii)	$t_1 = 1.6/4$	B1ft		ft acceleration
					(can be scored in (ii))
			M1		For using $0 = 1.6 - gt_2$
		Time taken is 0.56 s	A1	3	From $t_1 + t_2 = 0.4 + 0.16$
		townstive for most (!!!)			
	(Alt	ternative for part (iii))			For charming that the assessed area 1:-
					For observing that the average speed is
					the same for each of the two phases and
			3.71		equal to $(2 + 1) \cdot (2 - 1)$
	•		M1		$(0 + 1.6)/2 \text{ ms}^{-1}$
	-	$t_1 + t_2 = (s_1 + s_2)/0.8$	A1	2	
	Tim	te taken is 0.56 s	A1	3	FO: 11 1 C O 12
					[Similarly for finding $s_1 + s_2$ if ans(iii) is found before ans(ii)]
				•	
	(Alt	ternatively for parts ii and iii using v–t graph)			
			M1		Use of gradient to find t <sub>1</sub> or t <sub>2</sub>
	t. =	$1.6/4$ and $t_2 = 1.6/10$	A1		
		$\frac{1.074 \text{ and } t_2 - 1.0710}{1.084 \text{ and } t_3 - 1.0810}$	A1		
	1 11111	ic taken 15 0.305	$\Delta 1$		For use of area to find
			M1		$s_1$ or $s_2$ or $s_1 + s_2$
			1411		51 01 52 01 51 + 52
	ç. —	$0.4 \times 1.6/2$ or $s_0 = 0.16 \times 1.6/2$			
	$s_1 =$	$0.4 \times 1.6/2$ or $s_2 = 0.16 \times 1.6/2$ or $s_1 + s_2 = (0.4 + 0.16) \times 1.6/2$	Δ1		
		$0.4 \times 1.6/2$ or $s_2 = 0.16 \times 1.6/2$ or $s_1 + s_2 = (0.4 + 0.16) \times 1.6/2$ ght is $0.448$ m	A1 A1	6	

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		M1		For using $v(t) = \dot{s}(t)$
	$v = 1.2t - 0.012t^2$	A1		
				For using $a(t) = \dot{v}(t)$ and evaluating
	$[a(50) = 1.2 - 0.024 \times 50]$	M1		a(50)
	a = 0	<b>A</b> 1		AG
	V = 30	B1	5	
(ii)	$s_1 = 0.6 \times 50^2 - 0.004 \times 50^3 \ (= 1000)$	B1		
	$\left[\frac{1000 + s_2}{50 + t_2} = 27.5\right]$	M1		For using 'average speed = total distance /total time'
	$[1000 + 30t_2 = 27.5(50 + t_2)]$	M1		For substituting $s_2 = Vt_2$ and attempting to solve for $t_2$
	$t_2 = 150$	A1		
	t = 200	A1	5	ft 50 + t <sub>2</sub> (requires both M marks)
 (Al:	tornative for part (ii)		•	
		<b>D</b> 1		
s <sub>1</sub> -	0.0 \(^{30} - 0.004 \(^{30} \) (- 1000)	ы		For using 'average speed = total distance
Γ(10	$(000 + s_2)/t = 27.5$	M1		/total time' with $t_2 = t - 50$
- 1	-	A1ft		(ft V and $s_1$ )
[27.	5t = 1000 + 30(t - 50)	M1		For attempting to solve for t
-	, /=	A1	5	1 0
	(Alt s <sub>1</sub> = [(10 (100 [27.	$[a(50) = 1.2 - 0.024 \times 50]$ $a = 0$ $V = 30$ (ii) $s_1 = 0.6 \times 50^2 - 0.004 \times 50^3 (= 1000)$ $\left[\frac{1000 + s_2}{50 + t_2} = 27.5\right]$ $[1000 + 30t_2 = 27.5(50 + t_2)]$ $t_2 = 150$	$ [a(50) = 1.2 - 0.024 \times 50] $ $ a = 0 $ $ V = 30 $ $ A1$ $ B1 $ $ (ii)                                  $	$ [a(50) = 1.2 - 0.024 \times 50] $ $ a = 0 $ $ V = 30 $ $ (ii)                                  $